# (Basic Linear Algebra)

#### **Inverse Matrix**

Inverse of a 2×2 matrix

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix}^{-1} = \frac{1}{ad - bc} \begin{pmatrix} d & -b \\ -c & a \end{pmatrix}$$
 (0.10)

## Determinant

Determinant of a 2×2 matrix

$$\begin{vmatrix} a & b \\ c & d \end{vmatrix} = ad - bc \tag{0.11}$$

Determinant of a 3×3 matrix

$$\begin{vmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{vmatrix} = a_{11}a_{22}a_{33} + a_{21}a_{32}a_{13} + a_{31}a_{12}a_{23} \\ -a_{11}a_{32}a_{23} - a_{21}a_{12}a_{33} - a_{31}a_{22}a_{13} \end{vmatrix} = a_{11}a_{22}a_{33} + a_{21}a_{22}a_{23} - a_{21}a_{12}a_{33} - a_{31}a_{22}a_{13}$$

$$\begin{vmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{vmatrix} = a_{11}a_{22}a_{33} - a_{31}a_{22}a_{13}$$

$$(0.12)$$

## Eigenvalue and Eigenvector

The eigenvalues,  $\lambda_1$ ,  $\lambda_2$ , ...,  $\lambda_n$ , of *n*-dimensional square matrix **A** can be calculated as the solutions to the eigen equation,

$$|\mathbf{A} - \lambda \mathbf{E}| = 0 \tag{0.13}$$

The corresponding eigenvector  $\mathbf{s}_i$  can be obtained from the definition,

$$\mathbf{A}\mathbf{s}_i = \lambda_i \mathbf{s}_i \tag{0.14}$$

For example for a 2×2 matrix,  $\mathbf{A} = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$ , the eigen equation is

$$|\mathbf{A} - \lambda \mathbf{E}| = \begin{vmatrix} a - \lambda & b \\ c & d - \lambda \end{vmatrix} = (a - \lambda)(d - \lambda) - bc = 0$$

#### (Arrhenius Equation)

The temperature dependence of rate constants can be expressed by the Arrhenius equation or the modified Arrhenius equation.

$$k = A \exp\left(-\frac{E_{\rm a}}{RT}\right)$$
 Arrhenius equation (0.15)

$$k = AT^b \exp\left(-\frac{E_a}{RT}\right)$$
 Modified Arrhenius equation (0.16)

#### (Schedule)

- [5] June 22 (Wed) 8:30~
- [6] June 27 (Mon) 13:00~
- [7] June 29 (Wed) 8:30~
- [8] July 4 (Mon) 13:00~ [Problem-2] <u>Due Date: 17:00 July 19</u> (to the box in the dept. office)
- # The paper (report) must be submitted until the due date.
- # Submissions via e-mail will not be accepted.